Solubility of Benzil in Organic Nonelectrolyte Solvents. Comparison of Observed Versus Predicted Values Based upon Mobile Order Theory

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SOLUBILITY OF BENZIL IN ORGANIC NONELECTROLYTE SOLVENTS. COMPARISON OF OBSERVED VERSUS PREDICTED VALUES BASED UPON MOBILE ORDER THEORY

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Experimental solubilities are reported at 25.0 °C for benzil dissolved in twenty three different organic nonelectrolyte solvents containing ester-, ether-, chloro-, hydroxy- and methyl-functional groups. Results of these measurements combined with our previously published benzil solubility data in benzene, toluene, dibutyl ether, carbon tetrachloride and saturated hydrocarbons, are used to test the applications and limitations of expressions derived from Mobile Order theory. For the 30 solvents for which predictions could be made computations show that Mobile Order theory does provide fairly reasonable (although by no means perfect) estimates of the saturation mole fraction solubilities. Average absolute deviation between predicted and observed values is circa 31%. In comparison, the average absolute deviation increases significantly to 1500% when ideal solution behavior is assumed.

INTRODUCTION

Solid-liquid equilibrium data of organic nonelectrolyte systems are becoming increasingly important in the petroleum industry, particularly in light of present trends towards heavier feedstocks and known

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carcinogenicity/mutagenicity of many of the larger polycyclic aromatic compounds. Solubility data for a number of polycyclic aromatic hydrocarbons (e.g., anthracene and pyrene) and hetero-atom polynuclear aromatics (e.g., carbazole, dibenzothiophene and xanthene) have been published in the recent chemical literature (for listing of references see Acree [1–3]). Despite efforts by experimentalists and scientific organizations, both in terms of new experimental measurements and critically-evaluated data compilations, there still exist numerous systems for which solubility data are not readily available.

To address this problem, researchers have turned to group contribution methods and semi-empirical expressions to predict desired quantities. Group contribution methods have proved fairly successful in estimating solid solubility in pure and binary solvent mixtures from structural information [4–11]. Practical application though, is limited to systems for which all group interaction parameters are known. Interaction parameters can be evaluated from liquid-vapor, liquid-liquid and solid-liquid equilibria data. It is important that the data base contain as many different functional groups as possible, preferably with adequate representation from both mono- and multi-functional solute/solvent molecules to permit evaluation of potential synergistic effects. The data base should contain sufficient experimental values near infinite dilution in the event that one wishes to determine separate interaction parameters for finite concentration and infinite dilution activity coefficient predictions. For this reason, we have measured benzil solubilities in 23 different organic solvents. Functional groups represented include esters, ethers, hydroxy, methyl and chloroalkanes. These measurements will supplement our previously reported [12–17] benzil solubility data in benzene, toluene, carbon tetrachloride, dibutyl ether, methyl tert-butyl ether and saturated alkane hydrocarbon solvents, and will be used to further test the applications and limitations of predictive expressions derived from Mobile Order theory.

MATERIALS AND METHODS

Benzil (Aldrich, 98%) was recrystallized several times from methanol. Butyl acetate (Aldrich, 99.8 + %), 1-pentanol (Aldrich, 99 + %), 1,2-dichloroethane (Aldrich, 99 + %, anhydrous), 1,4-dioxane (Aldrich,

99.8+ %), ethyl acetate (Aldrich, 99.9%), 1-chlorobutane (Aldrich, 99.9+ %), ethanol (Aaper Alcohol and Chemical Company, absolute), methanol (Aldrich, 99.9+ %), 1-propanol (Aldrich 99+ %, anhydrous), 2-propanol (Aldrich 99+ %, anhydrous), 1-butanol (Aldrich HPLC, 99.8+ %), 2-butanol (Aldrich 99+ %, anhydrous), 1-hexanol (Alfa Aesar, 99+ %), 1-heptanol (Alfa Aesar, 99+ %), 2-methyl-2-butanol (Acros, 99+ %), 2-methyl-1-propanol (Aldrich 99+ %, anhydrous), 3-methyl-1-butanol (Aldrich 99+ %, anhydrous), 1-octanol (Aldrich 99+ %, anhydrous), 2-pentanol (Acros 99+ %), 4-methyl-2-pentanol (Acros 99+ %), tetrahydrofuran (Sigma-Aldrich, 99.9+ %, HPLC grade), 2-ethyl-1-hexanol (Aldrich, 99+ %) and cyclopentanol (Aldrich, 99%) were stored over molecular sieves before use. Gas chromatographic analysis showed solvent purities to be 99.7 mole percent or better.

Excess solute and solvent were placed in amber glass bottles and allowed to equilibrate in a constant temperature water bath at 25.0 ± 0.1 °C for at least three days (often longer). Attainment of equilibrium was verified both by repetitive measurements after a minimum of three additional days and by approaching equilibrium from supersaturation by pre-equilibrating the solutions at a higher temperature. Aliquots of saturated benzil solutions were transferred through a coarse filter into a tared volumetric flask to determine the amount of sample and diluted quantitatively with methanol for spectrophotometric anlysis at 390 nm on a Bausch and Lomb Spectronic 2000. Concentrations of the dilute solutions were determined from a Beer-Lambert law absorbance versus concentration working curve derived from measured absorbances of nine standard solutions of known molar concentrations ranging from 4.30×10^{-3} Molar to 2.15×10^{-2} Molar. The calculated molar absorptivity of $\varepsilon \approx 65.8$ L mol^{-1} cm^{-1} was constant over the concentration range. Experimental molar concentrations were converted to (mass/mass) solubility fractions by multiplying by the molar mass of benzil, volume(s) of volumetric flask(s) used and any dilutions required to place the measured absorbances on the Beer-Lambert law absorbance versus concentration working curve, and then dividing by the mass of the saturated solution analyzed. Mole fraction solubilities were computed from (mass/mass) solubility fractions using the molar masses of the solute and solvent. Experimental benzil solubilities, X_A^{sat}, in 23 organic solvents studied are listed in Table 1. Numerical values represent the average of

TABLE 1 Experimental Benzil Mole
Fraction Solubilities in Select Organic
Solvents at 25.0°C

Organic Solvent	X_A^{sat}
Tetrahydrofuran	0.2512
1,4-Dioxane	0.2101
1-Chlorobutane	0.1047
1,2-Dichloroethane	0.2264
Ethyl acetate	0.1455
Butyl acetate	0.1350
Methanol	0.00783
Ethanol	0.01031
1-Propanol	0.01184
2-Propanol	0.00831
1-Butanol	0.01306
2-Butanol	0.01103
2-Methyl-1-propanol	0.00969
1-Pentanol	0.01503
2-Pentanol	0.01274
3-Methyl-1-butanol	0.01214
2-Methyl-2-butanol	0.01673
1-Hexanol	0.01563
4-Methyl-2-pentanol	0.01282
1-Heptanol	0.01643
1-Octanol	0.01692
2-Ethyl-1-hexanol	0.01563
Cyclopentanol	0.01792

between four and eight independent determinations. Reproducibility
ranged from $\pm 1.5\%$ for solvents having the lower mole fraction solubili-
ties to $\pm 2.5\%$ for solvents having the larger benzil solubilities, where an
additional dilution was necessary to keep the measured absorbances
within the Beer-Lambert law region.

RESULTS AND DISCUSSION

Solvents studied include both noncomplexing alkanes and self-associating
alcohols. Of the many solution models proposed in recent years, Mobile
Order theory is perhaps the only one that is capable of describing solute
behavior in such a wide range of solvent mixtures. The basic model
[18–25] assumes that all molecular groups perpetually move, and that
neighbors of a given kind of external atom in a molecule constantly change
identity. All molecules of a given kind dispose of the same volume, equal to

the total volume B of the liquid divided by the number N_A of molecules of the same kind, i.e., Dom $A = V/N_A$. The center of this domain perpetually moves. The highest mobile disorder is achieved whenever groups visit all parts of their domain without preference. Preferential contacts lead to deviations with respect to this "random" visiting. This is especially true in the case of hydrogen-bonding as specific interactions result in a specific orientation of the "donor" molecule with respect to an adjacent "acceptor" molecule.

In the case of an inert crystalline solute dissolved in a self-associating solvent, Mobile Order theory expresses the volume fraction saturation solubility, ϕ_A^{sat}, as

$$\ln \phi_A^{sat} = \ln a_A^{solid} - 0.5 \, (1 - V_A/V_{solvent}) \, \phi_{solvent}$$

$$+ 0.5 \, \ln \, [\phi_A^{sat} + \phi_{solvent}(V_A/V_{solvent})] - \phi_{solvent}^2$$

$$V_A(\delta_A' - \delta_{solvent}')^2 \, (RT)^{-1} - r_{solvent}(V_A/V_{solvent})\phi_{solvent} \quad \text{(Eqn. 1)}$$

where the $r_{solvent} \, (V_A/V_{solvent}) \, \phi_{solvent}$ term represents the contributions resulting from hydrogen-bond formation between the solvent molecules. For most of the published applications, $r_{solvent}$ was assumed to be unity for strongly associated solvents with single hydrogen-bonded chains such as monofunctional alcohols, to be two for water or diols, and to equal zero for non-associated solvents such as saturated hydrocarbons. A more exact value for alcoholic solvents can be calculated based upon

$$r_{solvent} = (K_{solvent} \, \phi_{solvent}/V_{solvent})/(1 + K_{solvent} \, \phi_{solvent}/V_{solvent}) \quad \text{(Eqn. 2)}$$

with a numerical value of $K_{solvent} = 5,000 \text{ cm}^3 \text{ mol}^{-1}$ assumed for all monofunctional alcohols.

If complexation does occur between the crystalline solute and solvent

$$\ln \phi_A^{sat} = \ln a_A^{solid} - 0.5 \, (1 - V_A/V_{solvent}) \, \phi_{solvent}$$

$$+ 0.5 \ln [\phi_A^{sat} + \phi_{solvent}(V_A/V_{solvent})] - \phi_{solvent}^2 \, V_A(\delta_A' - \delta_{solvent}')^2 (RT)^{-1}$$

$$+ \ln[1 + \phi_{solvent}(K_{A \, solvent}/V_{solvent})] \quad \text{(Eqn. 3)}$$

then an additional tern involving the solute-solvent equilibrium constant, $K_{A \, \text{Solvent}}$, must be introduced to describe the solubility enhancement that arises as a result of specific interactions. A slightly more complex expression applies in the case of solute complexation with a self-associating solvent. The symbols δ'_A and δ'_{solvent} denote the modified solubility parameters of the solute and solvent, respectively, V_i is the molar volume, and a_A^{solid} is the activity of the solid solute. This latter quantity is defined as the ratio of the fugacity of the solid to the fugacity of the pure hypothetical supercooled liquid. The numerical value of a_A^{solid} can be computed from

$$\ln a_A^{\text{solid}} = -\Delta H_A^{\text{fus}} (T_{\text{mp}} - T)/(RTT_{\text{mp}}) \qquad \text{(Eqn. 4)}$$

the solute's molar enthalpy of fusion, ΔH_A^{fus}, at the normal melting point temperature, T_{mp}. Contributions from nonspecific interaction are incorporated into Mobile Order theory through the $\phi_{\text{solvent}}^2 \, V_A$ $(\delta'_A - \delta'_{\text{solvent}})^2 \, (RT)^{-1}$ term. Ruelle and coworkers [21–25] have presented a very impressive set of comparisons between experimental and predicted for anthracene, naphthalene, pyrene (see also Powell et al. [26]), biphenyl, carbazole, benzil, p-benzoquinone, tricosane, octacosane, 10-nonadecanone, 11-heneicosanone, and 12-tricosanone in a wide range of both noncomplexing and complexing solvents to document the predictive ability of Mobile Order theory.

Predictive application of Eqns. (1) and (3) is relatively straight-forward. First, an average numerical value of $\delta'_{\text{benzil}} = 21.69 \ \text{MPa}^{1/2}$ is computed by requiring that each equation (with $r_{\text{solvent}} = 0$ and/or $K_{A \, \text{Solvent}} = 0$) perfectly describes our previously published [12, 13] benzil mole fraction solubility data in n-hexane ($\delta'_{\text{benzil}} = 21.70 \ \text{MPa}^{1/2}$), n-heptane ($\delta'_{\text{benzil}} = 21.64 \ \text{MPa}^{1/2}$), and n-octane ($\delta'_{\text{benzil}} = 21.72 \ \text{MPa}^{1/2}$). The numerical value of of $a_A^{\text{solid}} = 0.224$ is calculated using Eqn. (4) with $\Delta H_A^{\text{fus}} = 19{,}480 \ \text{J mol}^{-1}$,[27] and $T_{\text{mp}} = 368.3 \ K$. The molar volume of the hypothetical subcooled liquid solute, $V_{\text{benzil}} = 183 \ \text{cm}^3 \ \text{mol}^{-1}$, was estimated from the density of the liquid at 102 °C [27] and the coefficient of thermal expansion for benzophenone calculated over the range 50–95 °C [28] This value is in reasonable agreement with limiting partial molar volumes of benzil in benzene ($V_{\text{benzil}} = 179 \ \text{cm}^3 \ \text{mol}^{-1}$), toluene ($V_{\text{benzil}} = 179 \ \text{cm}^3 \ \text{mol}^{-1}$) and nitrobenzene ($V_{\text{benzil}} = 183 \ \text{cm}^3 \ \text{mol}^{-1}$) calculated from experimental data reported by Tyrer [29].

Table 2 summarizes the predictive ability of Mobile Order theory for the 30 different organic solvents for which both benzil solubility data and modified solubility parameters could be found. Solvent molar volumes and modified solubility parameters are listed in Table 3. The modified solubility parameters account for only nonspecific interactions, and in the case of the alcoholic solvents the hydrogen-bonding contributions have been removed. Numerical values of $\delta'_{solvent}$ were obtained from published compilations [21, 22, 25], and were either

TABLE 2   Comparison Between Experimental Benzil Mole Fraction Solubilities and Predicted Values Based Upon Mobile Order Theory

Organic Solvent	$(X_A^{sat})^{exp}$	$(X_A^{sat})^{calc}$	% Dev[a]
n-Hexane	0.00570[13]	0.00575	0.8
n-Heptane	0.00659[12]	0.00623	− 5.5
	0.00654[13]	0.00623	− 4.7
n-Octane	0.00726[12]	0.00737	1.5
n-Nonane	0.00794[16]	0.00939	18.3
Cyclohexane	0.01068[12]	0.00818	− 23.4
	0.01072[13]	0.00818	− 23.7
Methylcyclohexane	0.01128[15]	0.00927	− 17.8
Cyclooctane	0.01454[12]	0.01378	− 5.2
	0.01485[16]	0.01378	− 7.2
2,2,4-Trimethylpentane	0.00587[12]	0.00412	− 29.8
tert-Butylcyclohexane	0.01114[16]	0.01441	29.4
Benzene	0.1804[13]	0.1895	5.0
Toluene	0.1504[13]	0.1295	− 13.9
Carbon tetrachloride	0.08082[12]	0.0743	− 8.1
	0.0804[13]	0.0743	− 7.6
1-Chlorobutane	0.1047	0.0732	− 30.1
1,2-Dichloroethane	0.2264	0.2422	7.0
Dibutyl ether	0.03351[15]	0.07205	115.0
Tetrahydrofuran	0.2512	0.2105	− 16.2
1,4-Dioxane	0.2101	0.2388	13.7
Ethyl acetate	0.1455	0.2302	58.8
Butyl acetate	0.1350	0.1918	42.1
Methanol	0.00783	0.01098	40.2
Ethanol	0.01031	0.00578	− 43.9
1-Propanol	0.01184	0.00456	− 61.5
2-Propanol	0.00831	0.00831	0.0
1-Butanol	0.01306	0.00848	− 35.1
2-Butanol	0.01103	0.00563	− 49.0
2-Methyl-1-propanol	0.00969	0.00390	− 59.8
1-Pentanol	0.01503	0.00857	− 43.0
1-Hexanol	0.01563	0.00727	− 53.5
1-Heptanol	0.01643	0.00837	− 49.1
1-Octanol	0.01692	0.00935	− 44.7

[a] Deviations (%) = $100 [(X_A^{sat})^{calc} − (X_A^{sat})^{exp}] / (X_A^{sat})^{exp}$.

TABLE 3   Solvent and Solute Properties Used in Mobile Order Predictions

Component (i)	$V_i/(cm^3 mol^{-1})$	$\delta'_i/(MPa^{1/2})^a$
n-Hexane	131.51	14.56
n-Heptane	147.48	14.66
n-Octane	163.46	14.85
n-Nonane	179.7	15.07
Cyclohexane	108.76	14.82
Methylcyclohexane	128.32	15.00
2,2,4-Trimethylpentane	166.09	14.30
Cyclooctane	134.9	15.40
tert-Butylcyclohexane	173.9	15.50
Benzene	89.4	18.95
Toluene	106.84	18.10
Carbon tetrachloride	97.1	17.04
1,2-Dichloroethane	78.8	20.99
1-Chlorobutane	105.0	17.12
Dibutyl ether	170.3	17.45
1,4-Dioxane	85.8	20.89
Tetrahydrofuran	81.4	19.30
Ethyl acetate	98.5	20.79
Butyl acetate	132.5	19.66
Methanol	40.7	19.25
Ethanol	58.7	17.81
1-Propanol	75.10	17.29
2-Propanol	76.90	17.60
1-Butanol	92.00	17.16
2-Butanol	92.4	16.60
2-Methyl-1-propanol	92.8	16.14
1-Pentanol	108.6	16.85
1-Hexanol	125.2	16.40
1-Heptanol	141.9	16.39
1-Octanol	108.6	16.38
Benzil[b]	183.0	21.69[c]

[a] Tabulated values are taken from a compilation given in Ruelle et al. [21,22,25].

[b] The numerical value of $a_A^{solid} = 0.224$ was calculated from the molar enthalpy of fusion, $\Delta H_A^{fus} = 19,480 \, J \, mol^{-1}$, [27] at the normal melting point temperature of the solute, $T_{mp} = 368.3 \, K$.

[c] Numerical value was calculated using the measured benzil mole fraction solubilities in n-hexane, n-heptane and n-octane, in accordance with Eqns. (1) and (3); with $r_{solvent} = 0$ and/or $K_{A \, Solvent} = 0$.

deduced by regressing actual solubility data of solid n-alkanes in organic solvents in accordance with the configurational entropic model of Huyskens and Haulait-Pirson [30] or estimated using known values for similar organic solvents. Examination of the entries in

Table 2 reveals that Mobile Order theory does provide fairly reasonable (though by no means perfect) estimates of the solubility behavior of benzil in a wide range of organic solvents. Average absolute deviation between predicted and observed values is circa 31%. It should be noted that Ruelle and coworkers [25] previously presented a similar comparison involving Mobile Order theory; however, the authors' solvent set included primarily saturated alkane hydrocarbons. Our comparison is more complete in that 18 additional solvents are considered. Readers are reminded that in evaluating the applicability of Mobile Order theory one must realize that many of these particular systems are highly non-ideal, and that the experimental solubility data covers over a 35-fold range in mole fraction. Had an ideal solution been assumed, then the predicted mole fraction solubility would be $X_A^{sat} = a_A^{solid} = 0.224$ for each solvent. The ideal solution approximation corresponds to a considerably larger average absolute deviation of 1500% between predicted and observed values.

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